Non-Euclidean distances in **secr** 5.2

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Introduction

Spatially explicit capture–recapture (SECR) entails a distance-dependent observation model: the expected number of detections (λ) or the probability of detection (g) declines with increasing distance between a detector and the home-range centre of a focal animal. 'Distance' here usually, and by default, means the Euclidean distance $d = \sqrt{(x_1 - x_2)^2 + (y_1 - y_2)^2}$. The observation model can be customised by replacing the Euclidean distance with one that 'warps' space in some ecologically meaningful way. There are innumerable ways to do this. One is the a non-Euclidean 'ecological distance' envisioned by Royle et al. (2013).

This document shows how to define and use non-Euclidean distances in secr 5.2. An appendix gives example secr code for the non-Euclidean SECR analysis of Sutherland et al. (2015).

Basics

Non-Euclidean distances are defined in **secr** by setting the 'userdist' component of the 'details' argument of **secr.fit**. The options are (i) to provide a static $K \times M$ matrix containing the distances between the K detectors and each of the M mask points, or (ii) to provide a function that computes the distances dynamically. A static distance matrix can allow for barriers to movement. Providing a function is more flexible and allows the estimation of a parameter for the distance model, but evaluating the function for each likelihood slows down model fitting.

Static userdist

A pre-computed non-Euclidean distance matrix may incorporate constraints on movement, particularly mapped barriers to movement, and this is the most obvious reason to employ a static userdist. The function **nedist** builds a suitable matrix.

As an example, take the 1996 DNA survey of the grizzly bear population in the Central Selkirk mountains of British Columbia by Mowat and Strobeck $(2000)^1$. Their study area was partly bounded by lakes and reservoirs that we assume are rarely crossed by bears. To treat the lakes as barriers in a SECR model we need a matrix of hair snag – mask point distances for the terrestrial (non-Euclidean) distance between each pair of points.

We start with the hair snag locations CStraps and a SpatialPolygonsDataFrame object BLKS_BC representing the large lakes (Fig. 1a). Buffering 30 km around the detectors gives a naive mask (Fig. 1b); we use a 2-km pixel size and reject points centred in a lake. The shortest dry path from many points on the naive mask to the nearest detector is much longer than the straight line distance.





¹Thanks to Garth Mowat for providing these data.

Fig. 1. (a) Central Selkirk grizzly bear hair snag locations (Mowat and Strobeck 2000), (b) Mask using naive 30-km buffer around hair snags, (c) Example map of dry-path distances from an arbitrary point, and (d) Efficient mask rejecting dry-path distances >30km.

We next calculate the matrix of all dry detector-mask distances by calling **nedist** that in turn uses functions from the R package **gdistance** (van Etten 2014). Missing pixels in the mask represent barriers to movement when their combined width exceeds a threshold determined by the adjacency rule in **gdistance**.

What do we mean by an adjacency rule? **gdistance** finds least-cost distances through a graph formed by joining 'adjacent' pixels. Adjacent pixels are defined by the argument 'directions', which may be 4 (rook's case), 8 (queen's case) or 16 (knight and one-cell queen moves) as in the **raster** function adjacent. The default in **nedist** is 'directions = 16' because that gives the best approximation to Euclidean distances when there are no barriers. The knight's moves are $\sqrt{5} \approx 2.24 \times$ cell width ('spacing'), so the width of a polygon intended to map a barrier should be at least $2.24 \times$ cell width.

Some of the BC lakes are narrow and less than 4.48 km wide. To ensure these act as barriers we could simply reduce the spacing of our mask, but that would slow down model fitting. The alternative is to retain the 2-km mask for model fitting and to define a finer (0.5-km) mask purely for the purpose of computing distances²:

The first argument of **nedist** provides the rows of the distance matrix and the second argument the columns; the third (if present) defines an alternative mask on which to base the calculations. To verify the computation, map the distance from a chosen detector i to every point in a mask. Here is a short function to do that; see Fig. 1c for an example.

```
dmap <- function (traps, mask, userd, i = 1, ...) {
    if (is.na(i)) i <- nearesttrap(unlist(locator(1)), traps)
    covariates(mask) <- data.frame(d = userd[i,])
    covariates(mask)$d[!is.finite(covariates(mask)$d)] <- NA
    plot(mask, covariate = "d", ...)
    points(traps[i,], pch = 3, col = "red")
}
dmap(CStraps, CSmask2000, userd, dots = F, scale = 0.001, title = "distance km")</pre>
```

At this point we could simply use 'userd' as our userdist matrix. However, CSmask2000 now includes a lot of points that are further than 30 km from any detector. It is better to drop these points and the associated columns of 'userd' (Fig. 1d):

```
OK <- apply(userd, 2, min) < 30000
CSmask2000b <- subset(CSmask2000, OK)
userd <- userd[,OK]
```

Finally, we can fit a model using the non-Euclidean distance matrix:

```
CSa <- secr.fit(CS_sexcov_all, mask = CSmask2000b, details = list(userdist = userd))
predict(CSa)</pre>
```

For completeness, note that Euclidean distances may also be pre-calculated, using the function edist. By default, secr.fit uses that function internally, and there is usually little speed improvement when the calculation is done separately.

²Mixing 2-km and 0.5-km cells carries a slight penalty: the centres of a few 2-km cells (<1%) do not lie in valid 0.5-km cells; these become inaccessible (infinite distance from all detectors) and are silently dropped in a later step.

Dynamic userdist

The userdist function takes three arguments. The first two are simply 2-column matrices with the coordinates of the detectors and animal locations (mask points) respectively. The third is a habitat mask (this may be the same as xy2). The function has this form:

```
mydistfn <- function (xy1, xy2, mask) {
    if (missing(xy1)) return(charactervector)
    ...
    distmat # return nrow(xy1) x nrow(xy2) matrix
}</pre>
```

Computation of the distances is entirely under the control of the user – here we indicate that by '...'. The calculations may use cell-specific values of two 'real' parameters 'D' and 'noneuc' that as needed are passed by secr.fit as covariates of the mask. 'D' is the usual cell-specific expected density in animals per hectare. 'noneuc' is a special cell-specific 'real' parameter used only here: it means whatever the user wants it to mean.

Whether 'noneuc', 'D' or other mask covariates are needed by mydistfn is indicated by the character vector returned by mydistfn when it is called with no arguments. Thus, charactervector may be either a zero-length character vector or a vector of one or more parameter names ("noneuc", "D", c("noneuc", "D")).

'noneuc' has its own link scale (default 'log') on which it may be modelled as a linear function of any of the predictors available for density (x, y, x2, y2, xy, session, Session, g, or any mask covariate – see secr-densitysurfaces.pdf). It may also, in principle, be modelled using regression splines (Borchers and Kidney in prep.), but this is untested. When the model is fitted by **secr.fit**, the beta parameters for the 'noneuc' submodel are estimated along with all the others. To make noneuc available to userdist, ensure that it appears in the 'model' argument. Use the formula noneuc ~ 1 if noneuc is constant.

The function may compute least-cost paths via intervening mask cells using the powerful **igraph** package (Csardi and Nepusz 2006). This is most easily accessed with Jacob van Etten's package **gdistance**, which in turn uses the RasterLayer S4 object class from the package **raster**. To facilitate this we include code in **secr** to treat the 'mask' S3 class as a virtual S4 class, and provide a method for the function 'raster' to convert a mask to a RasterLayer.

If the function generates any bad distances (negative, infinite or missing) these will be replaced by 1e10, with a warning.

Examples

We use annotated examples to show how the userdist function may be used to define different models. For illustration we use the Orongorongo Valley brushtail possum dataset from February 1996 (see OVpossum in secr-manual.pdf). The data are captures of possums over 5 nights in single-catch traps at 30-m spacing. We start by extracting the data, defining a habitat mask, and fitting a null model:

The warning is routine: we will suppress it in later examples. The distance functions below are not specific to a particular study: each may be applied to other datasets.

1. Scale of movement σ depends on location of home-range centre

In this simple case we use the non-Euclidean distance function to model continuous spatial variation in σ . This cannot be done directly in **secr** because sigma is treated as part of the detection model, which does not allow for continuous spatial variation in its parameters. Instead we model spatial variation in 'noneuc' as a stand-in for 'sigma'

predict(fit1)

##		link	estimate	SE.estimate	1c1	ucl	
##	D	log	14.6843	1.091475	12.69615	16.9838	
##	lambda0	log	0.1085	0.009626	0.09123	0.1291	
##	noneuc	log	25.9243	1.301933	23.49554	28.6040	

We can take the values of noneuc directly from the mask covariates because we know xy2 and mask are the same points. We may sometimes want to use fn1 in context where this does not hold, e.g., when simulating data.

predict(fit1a)

 ##
 link estimate
 SE.estimate
 lcl
 ucl

 ##
 D
 log
 14.4619
 1.029689
 12.58050
 16.6248

 ##
 lambda0
 log
 0.1076
 0.009525
 0.09047
 0.1279

 ##
 noneuc
 log
 26.1254
 1.419877
 23.48742
 29.0596

We can verify the use of 'noneuc' in fn1 by using it to re-fit the null model:

predict(fit0)

```
##
           link estimate SE.estimate
                                          lcl
                                                   ucl
## D
                             1.003093 12.5447 16.4842
            log 14.3802
## lambda0
            log
                  0.1015
                             0.008948 0.0854 0.1206
## sigma
            log
                 27.3765
                             0.972969 25.5349 29.3508
predict(fit0a)
           link estimate SE.estimate
##
                                          1c1
                                                   11C]
## D
                14.3802
                             1.003093 12.5447 16.4842
            log
## lambda0
            log
                  0.1015
                             0.008948 0.0854 0.1206
## noneuc
            log
                 27.3764
                             0.972967 25.5349 29.3508
```

Here, fitting noneuc as a constant while holding sigma fixed is exactly the same as fitting sigma alone.

2. Scale of movement σ depends on locations of both home-range centre and detector

Hypothetically, detections at xy1 of an animal centred at xy2 may depend on both locations (this may also be seen as a approximation to the following case of continuous variation along the path between xy1 and xy2). To model this we need to retrieve the value of noneuc for both locations. Within fn2 we use addCovariates to extract the covariates of the mask (and hence noneuc) for each point in xy1 and xy2. The call to secr.fit is identical except that it uses fn2 instead of fn1:

predict(fit2)

link estimate SE.estimate lcl ucl ## D 14.5466 1.058030 12.61626 16.7722 log ## lambda0 log 0.1078 0.009549 0.09066 0.1282 ## noneuc 26.0233 1.351012 23.50723 28.8087 log

Tip: the value of noneuc reported by predict.secr is the predicted value at the centroid of the mask, because the model uses standardised mask coordinates.

3. Continuously varying σ using gdistance

A more elegant but slower approach is to find the least-cost path across the network of cells between xy1 and xy2, using noneuc (i.e. sigma) as the cell-specific cost weighting (large cell-specific sigma equates with greater 'conductance', the inverse of friction or cost). For this we use functions from the package **gdistance**, which in turn uses **igraph**.

```
fn3 <- function (xy1, xy2, mask) {</pre>
  if (missing(xy1)) return("noneuc")
  # warp distances to be proportional to int_along path sigma(x,y) dp
  # where p is path distance
  if (!require(gdistance))
    stop ("install package gdistance to use this function")
  # make raster from mask
  Sraster <- raster(mask, "noneuc")</pre>
  # Assume animals can traverse gaps: bridge gaps using global mean
  Sraster[is.na(Sraster[])] <- mean(Sraster[], na.rm = TRUE)</pre>
  # TransitionLayer
  tr <- transition(Sraster, transitionFunction = mean, directions = 16)</pre>
  tr <- geoCorrection(tr, type = "c", multpl = FALSE)</pre>
  # costDistance
  costDistance(tr, as.matrix(xy1), as.matrix(xy2))
}
fit3 <- secr.fit(ovposs, mask = ovmask, detectfn = "HHN", trace = FALSE,</pre>
                  details = list(userdist = fn3), model = noneuc ~ x + y + x2 + y2 + xy,
                 fixed = list(sigma = 1))
```

predict(fit3)

##		link	estimate	SE.estimate	lcl	ucl
##	D	log	14.4063	1.050021	12.49093	16.6154
##	lambda0	log	0.1076	0.009504	0.09053	0.1279
##	noneuc	log	26.4338	1.364355	23.89218	29.2459

The **gdistance** function **costDistance** uses a TransitionLayer object that essentially describes the connections between cells in a RasterLayer. In **transition** adjacent cells are assigned a positive value for 'conductance' and all other cells a zero value. Adjacency is defined by the directions argument as 4 (rook's case), 8 (queen's case), 16 (knight and one-cell queen moves) and possibly other values (see ?adjacent in **gdistance**). Values < 16 can considerably distort distances even if conductance is homogeneous. **geoCorrection** is needed to allow for the greater separation $(\times \sqrt{2})$ of cell centres measured along diagonals.

In ovmask there are two forest blocks separated by a shingle stream bed and low scrub that is easily crossed by possums but does not count as 'habitat'. Habitat gaps are assumed in **secr** to be traversible. The opposite is assumed by **gdistance**. To coerce **gdistance** to behave like **secr** we here temporarily fill in the gaps.

The argument 'transitionFunction' determines how the conductance values of adjacent cells are combined to weight travel between them. Here we simply average them, but any other single-valued function of 2 inputs can be used.

Integrating along the path (fn3) takes about 3.6 times as long as the approximation (fn2) and gives quite similar results.

4. Density-dependent σ

A more interesting variation makes sigma a function of the cell-specific density, which may vary independently across space (Efford et al. 2015). Specifically, $\sigma(x, y) = k/\sqrt{D(x, y)}$, where k is the fitted parameter (noneuc).

```
fn4 <- function (xy1, xy2, mask) {
    if(missing(xy1)) return(c("D", "noneuc"))
    if (!require(gdistance))
      stop ("install package gdistance to use this function")
    # make raster from mask
    D <- covariates(mask)$D</pre>
```

predict(fit4)

 ##
 link
 estimate
 SE.estimate
 lcl
 ucl

 ##
 D
 log
 15.4548970
 1.638571525
 12.56236531
 19.0134449

 ##
 lambda0
 log
 0.1066912
 0.009407833
 0.08978763
 0.1267771

 ##
 noneuc
 log
 103.2281764
 5.033253378
 93.82521347
 113.5734842

predict(fit4a)

##		link	estimate	SE.estimate	lcl	ucl
##	D	log	15.7641512	1.766438512	12.66447851	19.6224789
##	lambda0	log	0.1068068	0.009416593	0.08988723	0.1269111
##	noneuc	log	103.0827973	5.008734347	93.72407828	113.3760213

plot(predictDsurface(fit4a))
plot(traps(ovposs), add=T)
lines(leftbank)



5. Habitat model for connectivity

Yet another possibility, in the spirit of Royle et al. (2013), is to model conductance as a function of habitat covariates. As usual in **secr** these are stored as one or more mask covariates. It is easy to add a covariate for forest type (*Nothofagus*-dominant 'beech' vs 'nonbeech') to our mask:

```
ovmask <- addCovariates(ovmask, ovforest[1:2,])</pre>
fit5 <- secr.fit(ovposs, mask = ovmask, detectfn = "HHN", trace = FALSE,</pre>
                 details = list(userdist = fn2), model = list(D ~ forest, noneuc ~ forest),
                 fixed = list(sigma = 1))
predict(fit5, newdata = data.frame(forest=c("beech", "nonbeech")))
## $`forest = beech`
##
           link
                  estimate SE.estimate
                                                lcl
                                                            ucl
                                         5.48570024 16.1935957
## D
                 9.4251372
                           2.65312644
            log
                 0.1011087
                            0.00893371
                                         0.08505983 0.1201855
## lambda0
            log
## noneuc
            log 29.5577354
                            3.40606292 23.59972290 37.0199143
##
## $`forest = nonbeech`
##
           link
                  estimate SE.estimate
                                                1c1
                                                            1101
## D
                           1.26793441 13.37985208 18.3627082
            log 15.6745118
                            0.00893371 0.08505983 0.1201855
## lambda0
            log 0.1011087
## noneuc
            log 27.2347531
                            1.03191593 25.28618197 29.3334824
```

Note that we have re-used the userdist function fn2, and allowed both density and noneuc (sigma) to vary by forest type. Strictly, we should have identified "forest" as a required covariate in the (re)definition of fn2, but this is obviously not critical.

A full analysis should also consider models with variation in lambda0. There is no simple way in **secr** to model continuous spatial variation in lambda0 as a function of home-range location (cf sigma in Example 1 above). However, variation in lambda0 at the point of detection may be modelled with detector-level covariates(secr-overview.pdf).

And the winner is...

Now that we have a bunch of fitted models, let's see which does the best:

```
AIC(fit0, fit0a, fit1, fit1a, fit2, fit3, fit4, fit4a, fit5, criterion = "AIC")[, -c(2,4,6)]
```

##				model	npar	AIC	dAIC	AICwt
##	fit4a		$D \sim s(x, y, k = 6)$	lambda0~1 noneuc~1	8	3098.129	0.000	0.4549
##	fit4	D~x	$+ y + x^{2} + y^{2} + xy$	lambda0~1 noneuc~1	8	3098.511	0.382	0.3758
##	fit1	D~1	lambda0~1 noneuc~x	$+ y + x^{2} + y^{2} + xy$	8	3101.833	3.704	0.0714
##	fit3	D~1	lambda0~1 noneuc~x	$+ y + x^{2} + y^{2} + xy$	8	3102.433	4.304	0.0529
##	fit2	D~1	lambda0~1 noneuc~x	$+ y + x^{2} + y^{2} + xy$	8	3103.540	5.411	0.0304
##	fit1a	D~1	lambda0~1 noneuc~x	+ y + x2 + y2 + xy	8	3104.991	6.862	0.0147
##	fit0		D~1	1 lambda0~1 sigma~1	3	3118.108	19.979	0.0000
##	fit0a		D~1	lambda0~1 noneuc~1	3	3118.108	19.979	0.0000
##	fit5		D~forest lambo	da0~1 noneuc~forest	5	3118.409	20.280	0.0000

... the model with a quadratic or spline trend in density and density-dependent sigma.

Notes

The 'real' parameter for spatial scale (σ) is lurking in the background as part of the detection model. User-defined non-Euclidean distances are used in the detection function just like ordinary Euclidean distances. This means in practice that they are (almost) always divided by (σ). Formally: the distance d_{ij} between an animal *i* and a detector *j* appears in all commonly used detection functions as the ratio $r_{ij} = d_{ij}/\sigma$ (e.g., halfnormal $\lambda = \lambda_0 \exp(-0.5r_{ij}^2)$ and exponential $\lambda = \lambda_0 \exp(-r_{ij})$).

What if I want non-Euclidean distances, but do not want to estimate noneuc? This is a perfectly reasonable request if sigma is constant across space and the distance computation is determined entirely by the habitat geometry, with no need for an additional parameter. If 'noneuc' is not included in the character vector returned by your userdist function when it is called with no arguments then noneuc is not modelled at all. (This is the default in **secrlinear**).

The initial value of 'noneuc' can be a problem. The argument 'start' of **secr.fit** may be a named, and possibly incomplete, list of real parameter values, so a call such as this is valid:

```
##
##
   secr.fit(capthist = captdata, model = noneuc ~ 1, start = list(noneuc = 25),
##
       fixed = list(sigma = 1), details = list(userdist = fn2),
       trace = FALSE)
##
   secr 5.2.0, 12:30:55 26 Jan 2025
##
##
## Detector type
                       single
## Detector number
                       100
## Average spacing
                       30 m
## x-range
                       365 635 m
## y-range
                       365 635 m
##
## N animals
                      76
                    :
## N detections
                    :
                      235
## N occasions
                    :
                      5
## Mask area
                      21.22711 ha
                    :
##
## Model
                      D~1 g0~1 noneuc~1
                    :
## User distances
                       dynamic (function)
                   :
## Fixed (real)
                       sigma = 1
                    :
## Detection fn
                    :
                      halfnormal
## Distribution
                    :
                      poisson
## N parameters
                    :
                       3
## Log likelihood
                    :
                       -759.0257
## AIC
                       1524.051
                    :
## AICc
                       1524.385
                    :
##
## Beta parameters (coefficients)
##
                beta
                         SE.beta
                                       1c1
                                                   ucl
## D
           1.7010686 0.11761472 1.470548
                                             1.9315892
  g0
##
          -0.9784938 0.13623904 -1.245517 -0.7114702
  noneuc 3.3798318 0.04441538 3.292779
##
                                             3.4668844
##
##
   Variance-covariance matrix of beta parameters
##
                      D
                                    g0
                                               noneuc
           0.0138332230
                          0.0001557834 -0.0009907546
## D
           0.0001557834
## g0
                          0.0185610769 -0.0033433785
  noneuc -0.0009907546 -0.0033433785 0.0019727258
##
##
## Fitted (real) parameters evaluated at base levels of covariates
```

##		link	estimate	SE.estimate	lcl	ucl
##	D	log	5.4797998	0.64674046	4.3516189	6.9004676
##	g0	logit	0.2731907	0.02705129	0.2234771	0.3292741
##	noneuc	log	29.3658325	1.30493806	26.9175717	32.0367723

We have ignored the parameter λ_0 . This is almost certainly a mistake, as large variation in σ without compensatory or normalising variation in λ_0 is biologically implausible and can lead to improbable results (Efford and Mowat 2014, Efford 2014).

It is intended that non-Euclidean distances should work with all relevant functions in **secr**. However, not all possible combinations have been tested, and not all make sense. Please report any problems.

You may be tempted to model 'noneuc' as a function of group - after all, D~g is permitted, right? Unfortunately, this will not work. There is only one pre-computed distance matrix, rather than a set of matrices, one per group.

References

Borchers, D. L. and Efford, M. G. (2008) Spatially explicit maximum likelihood methods for capture–recapture studies. *Biometrics* **64**, 377–385.

Borchers, D. L. and Kidney, D. J. (2014) Flexible density surface estimation using regression splines with spatially explicit capture-recapture data. In prep.

Csardi, G. and Nepusz, T. (2006) The igraph software package for complex network research. *InterJournal* **1695**. http://igraph.org.

Efford, M. G. (2014) Bias from heterogeneous usage of space in spatially explicit capture–recapture analyses. *Methods in Ecology and Evolution* **5**, 599–602.

Efford, M. G., Dawson, D. K., Jhala, Y. V. and Qureshi, Q. (2016) Density-dependent home-range size revealed by spatially explicit capture-recapture. *Ecography* **39**, 676–688.

Efford, M. G. and Mowat, G. (2014) Compensatory heterogeneity in capture–recapture data. *Ecology* **95**, 1341–1348.

Mowat, G. and Strobeck, C. (2000) Estimating population size of grizzly bears using hair capture, DNA profiling, and mark-recapture analysis. *Journal of Wildlife Management* **64**, 183–193.

Royle, J. A., Chandler, R. B., Gazenski, K. D. and Graves, T. A. (2013) Spatial capture–recapture models for jointly estimating population density and landscape connectivity. *Ecology* **94**, 287–294.

Sutherland, C., Fuller, A. K. and Royle, J. A. (2015) Modelling non-Euclidean movement and landscape connectivity in highly structured ecological networks. *Methods in Ecology and Evolution* **6**, 169–177.

van Etten, J. (2014) gdistance: distances and routes on geographical grids. R package version 1.1-5. https://CRAN.R-project.org/package=gdistance

Appendix. Implementation in secr of Sutherland et al. (2014) non-Euclidean simulation.

Sutherland et al. (2014) simulated SECR data from a population of animals whose movement was channeled to varying extents along a dendritic network (river system). Their model treated the habitat as 2-dimensional and shrank distances for pixels close to water and expanded them for pixels further away. Chris has kindly provided data for the network map and detector layout which we use here to emulate their simulations in **secr**. We assume an existing SpatialLinesDataFrame **sample.water** for the network, and a matrix of x-y coordinates for detector locations gridTrapsXY. rivers is a version of sample.water clipped to the habitat mask and used only for plotting.

```
# use package secrlinear to create a discretised version of the network,
# as a handy way to get distance to water
# loading this package also loads secr
library(secrlinear)
library(gdistance)
swlinearmask <- read.linearmask(data = sample.water, spacing = 100)</pre>
# generate secr traps object from detector locations
tr <- data.frame(gridTrapsXY*1000) # convert to metres</pre>
names(tr) <- c("x","y")</pre>
tr <- read.traps(data=tr, detector = "count")</pre>
# generate 2-D habitat mask
sw2Dmask <- make.mask(tr, buffer = 3950, spacing = 100)</pre>
d2w <- distancetotrap(sw2Dmask, swlinearmask)</pre>
covariates(sw2Dmask) <- data.frame(d2w = d2w/1000)</pre>
                                                        # km to water
## Warning: attribute variables are assumed to be spatially constant throughout
## all geometries
# plot distance to water
```

```
par(mar = c(1,6,1,6))
plot(sw2Dmask, covariate = "d2w", dots = FALSE)
plot(tr, add = TRUE)
plot(rivers, add = TRUE, col = "blue")
```



Fig. A1. Shaded plot of distance to water (d2w in km) with detector sites (red crosses) and rivers superimposed. Detector spacing 1.5 km N-S.

The distance function requires a value of the friction parameter 'noneuc' for each mask pixel. Distances are approximated using **gdistance** functions as before, except that we interpret the distance-to-water scale as 'friction' and invert that for **gdistance**.

The Royle et al. (2013) and Sutherland et al. (2014) models use an (α_0, α_1) parameterisation instead of (λ_0, σ) . Their α_2 translates directly to a coefficient in the **secr** model, as we'll see. We consider just one realisation of one scenario (the package **secreting manages** replicated simulations of multiple scenarios).

```
# parameter values from Sutherland et al. 2014
alpha0 <- -1  # implies lambda0 = invlogit(-1) = 0.2689414
sigma <- 1400
alpha1 <- 1 / (2 * sigma<sup>2</sup>)
alpha2 <- 5  # just one scenario from the range 0..10
K <- 10  # sampling over 10 occasions, collapsed to 1 occasion</pre>
```

Now we are ready to build a simulated dataset.

m m

summary(CH, moves = TRUE)

##	Object	cla	ass	ca	pthist	5
##	Detecto	or ·	type	co	unt	
##	Detecto	or i	number	64		
##	Average	e sj	pacing	13	85.714	l m
##	x-range	Э		16	98699	1708399
##	y-range	Э		23	87891	2398391
##						
##	Counts	by	occasion	ı		
##				1	Tota	L
##	n			37	37	7
##	u			37	37	7
##	f			37	37	7
##	M(t+1)			37	37	7
##	losses			0	()
##	detect	ion	S	109	109	9
##	detecto	ors	visited	33	33	3
##	detecto	ors	used	64	64	1
##						
##	Number	of	movement	ts p	er and	imal
##	0 1	2	3			

```
## 16 13 7 1
##
  Distance moved, excluding zero (m)
##
##
      Min. 1st Qu.
                               Mean 3rd Qu.
                    Median
                                                Max.
##
      1386
              1386
                       1443
                               1552
                                        1500
                                                3151
##
## Individual covariates
##
    sex
##
   F:21
##
  M:16
```

Model fitting is simple, but the default starting value for noneuc is not suitable and is overridden:

```
fitne1 <- secr.fit (CH, mask = sw2Dmask, detectfn = "HHN", binomN = 10,
  model = noneuc ~ d2w -1, details = list(userdist = userdfn1),
  start = list(D = 0.005, lambda0 = 0.3, sigma = 1000, noneuc = 100),
  trace = FALSE)
```

The warning from nlm indicates a potential problem, but the standard errors and confidence limits below look plausible (they could be checked by running again with method = "none"). Fitting is slow (5 minutes on an aging PC). This is partly because the mask is large (32384 pixels) in order to maintain resolution in relation to the stream network.

coef(fitne1)

```
##
                   beta
                           SE.beta
                                          lcl
                                                    ucl
## D
              -5.304155 0.18171360 -5.660308 -4.948003
## lambda0
              -1.138630 0.16982960 -1.471490 -0.805770
## sigma
               7.149075 0.09139487
                                    6.969944
                                              7.328205
## noneuc.d2w
               4.596125 0.50303378 3.610197
                                               5.582053
```

predict(fitne1)

```
      ##
      link
      estimate
      SE.estimate
      lcl
      ucl

      ##
      D
      log
      4.970895e-03
      9.107872e-04
      3.481446e-03
      7.097566e-03

      ##
      lambda0
      log
      3.202575e-01
      5.478374e-02
      2.295832e-01
      4.467438e-01

      ##
      sigma
      log
      1.272928e+03
      1.165824e+02
      1.064163e+03
      1.522647e+03

      ##
      noneuc
      log
      7.539491e+00
      1.687568e+00
      4.888109e+00
      1.162902e+01
```

region.N(fitne1)

 ##
 estimate
 SE.estimate
 lcl
 ucl
 n

 ##
 E.N
 160.9775
 29.49493
 112.7431
 229.8476
 37

 ##
 R.N
 160.9774
 26.62656
 118.7687
 224.9739
 37

The coefficient noneuc.d2w corresponds to alpha2. Estimates of predicted ('real') parameters D and lambda0, and the coefficient noneuc.d2w, and are comfortably close to the true values, and all true values are covered by the 95% CI.

We fit the 'noneuc' (friction) parameter through the origin (zero intercept; -1 in formula). The predicted value of 'noneuc' relates to the covariate value for the first pixel in the mask (d2w = 1.133 km), but in this zero-intercept model the meaning of 'noneuc' itself is obscure. In effect, the parameter alpha1 (or sigma) serves as the intercept; the same model may be fitted by fixing sigma (fixed = list(sigma = 1)) and estimating an intercept for noneuc (model = noneuc ~ d2w). In this case, 'noneuc' may be interpreted as the site-specific sigma (see also examples in the main text).

It is interesting to plot the predicted detection probability under the simulated model. For plotting we add the pdot value as an extra covariate of the mask. Note that pdot here uses the 'noneuc' value previously added as a covariate to sw2Dmask.



Fig. A2. Shaded plot of $p_{\cdot}(x, y)$ (probability animal is detected at least once). Detector sites and rivers as in Fig. A1. Animals living within the detector array and away from a river (about half the population within the array) stand very little chance of being detected because the model confines them to a small home range and λ_0 is constant.